# Interactive Imitation Learning

# **Sham Kakade and Wen Sun** CS 6789: Foundations of Reinforcement Learning

#### Announcements

Presentation: Dec 2, 7, 9

Final report: NeurIPS format Maximum 9 pages for main tex (not including references and appendix)



#### Recap

**Offline IL and Hybrid Setting:** 



#### **Offline IL and Hybrid Setting:**

#### Recap

#### Ground truth reward $r(s, a) \in [0, 1]$ is unknown; assume expert is a near optimal policy $\pi^{\star}$



#### **Offline IL and Hybrid Setting:**

We have a dataset

#### Recap

Ground truth reward  $r(s, a) \in [0,1]$  is unknown; assume expert is a near optimal policy  $\pi^{\star}$ 

$$\mathsf{t} \, \mathscr{D} = (s_i^\star, a_i^\star)_{i=1}^M \sim d^{\pi^\star}$$

**Interactive Imitation Learning Setting** 

#### **Today:**

**Interactive Imitation Learning Setting** 

Key assumption: we can query expert  $\pi^{\star}$  at any time and any state during training

#### **Today:**

**Interactive Imitation Learning Setting** 

Key assumption: we can query expert  $\pi^{\star}$  at any time and any state during training

(Recall that previously we only had an offline dataset  $\mathcal{D} = (s_i^{\star}, a_i^{\star})_{i=1}^M \sim d^{\pi^{\star}}$ )

#### **Today:**

# Recall the Main Problem from Behavior Cloning:

## No training data of "recovery" behavior

Learned Policy



# Intuitive solution: Interaction

# Use interaction to collect data where learned policy goes



# General Idea: Iterative Interactive Approach



**Updated Policy** 

All DAgger slides credit: Drew Bagnell, Stephane Ross, Arun Venktraman







**Supervised Learning** 

# DAgger: Dataset Aggregation [Ross11a] 1st iteration

**Execute**  $\pi_1$  and Query Expert





**Execute**  $\pi_1$  and Query Expert





#### **New Data**









**Execute**  $\pi_1$  and Query Expert





**New Data** 





#### 10

**Execute**  $\pi_1$  and Query Expert





**Execute**  $\pi_1$  and Query Expert



# DAgger: Dataset Aggregation [Ross11a] 2nd iteration

#### **Execute** $\pi_2$ and Query Expert



### [Ross11a] DAgger: Dataset Aggregation n<sup>th</sup> iteration

**Execute**  $\pi_{n-1}$  and Query Expert



# Success!



# Success!



# Success!



# Average Falls/Lap



# More fun than Video Games...



[Ross ICRA 2013] 17

# More fun than Video Games...



[Ross ICRA 2013] 17

# More fun than Video Games...



[Ross ICRA 2013] 17

Interactive Expert is expensive, especially when the expert is human...

But expert does not have to be human...

Interactive Expert is expensive, especially when the expert is human...

But expert does not have to be human...

**Example: high-speed off-road driving** [Pan et al, RSS 18, Best System Paper]



Fig. 4: The AutoRally car and the test track.

Interactive Expert is expensive, especially when the expert is human...

But expert does not have to be human...

**Example: high-speed off-road driving** [Pan et al, RSS 18, Best System Paper]



Fig. 4: The AutoRally car and the test track.

Goal: learn a racing control policy that maps from data on cheap on-board sensors (raw-pixel imagine) to low-level control (steer and throttle)

Interactive Expert is expensive, especially when the expert is human...

But expert does not have to be human...

**Example: high-speed off-road driving** [Pan et al, RSS 18, Best System Paper]



Fig. 4: The AutoRally car and the test track.

Goal: learn a racing control policy that maps from data on cheap on-board sensors (raw-pixel imagine) to low-level control (steer and throttle)



Steering + throttle

(a) raw image



**Example: high-speed off-road driving** [Pan et al, RSS 18, Best System Paper]

**Example: high-speed off-road driving** [Pan et al, RSS 18, Best System Paper]

Their Setup: At Training, we have expensive sensors for accurate state estimation and we have computation resources for MPC (i.e., high-frequency replanning)

**Example: high-speed off-road driving** [Pan et al, RSS 18, Best System Paper]

Their Setup: At Training, we have expensive sensors for accurate state estimation and we have computation resources for MPC (i.e., high-frequency replanning)

The MPC is the expert in this case!

**Example: high-speed off-road driving** [Pan et al, RSS 18, Best System Paper]

#### The MPC is the expert in this case!



Their Setup: At Training, we have expensive sensors for accurate state estimation and we have computation resources for MPC (i.e., high-frequency replanning)

#### Analysis of DAgger

First let's do a quick introduction of online no-regret learning

#### Learner



convex Decision set  ${\mathcal X}$ 

[Vovk92,Warmuth94,Freund97,Zinkevich03,Kalai05,Hazan06,Kakade08] Online Learning

. . .

### Adversary




Learner picks a decision  $x_0$ 

. . .

#### Learner



convex Decision set  ${\mathcal X}$ 







Learner picks a decision  $x_0$ 

. . .

#### Learner



convex Decision set  ${\mathcal X}$ 

Adversary picks a loss  $\mathscr{C}_0:\mathscr{X}\to\mathbb{R}$ 





Learner picks a decision  $x_0$ 

#### Learner



Adversary picks a loss  $\mathscr{C}_0:\mathscr{X}\to\mathbb{R}$ 

Learner picks a new decision  $x_1$ 

. . .

convex Decision set  ${\mathcal X}$ 

### Adversary



Learner picks a decision  $x_0$ 

#### Learner



Learner picks a new decision  $x_1$ 

. . .

Adversary picks a loss  $\ell_1 : \mathcal{X} \to \mathbb{R}$ 

convex Decision set  ${\mathcal X}$ 

Adversary picks a loss  $\mathscr{C}_0: \mathscr{X} \to \mathbb{R}$ 

### Adversary



Learner picks a decision  $x_0$ 

#### Learner



Learner picks a new decision  $x_1$ 

Adversary picks a loss  $\ell_1 : \mathcal{X} \to \mathbb{R}$ 

convex Decision set  ${\mathcal X}$ 



Adversary picks a loss  $\mathscr{C}_0: \mathscr{X} \to \mathbb{R}$ 

### Adversary



//\_1  $\operatorname{\mathsf{Regret}} = \sum_{t=0}^{\infty} \mathscr{\ell}_t(x_t) - \min_{x \in \mathscr{X}} \sum_{t=0}^{\infty} \mathscr{\ell}_t(x)$ 

. . .

#### A no-regret algorithm: Follow-the-Leader

At time step t, learner has seen  $\ell_0, \ldots \ell_{t-1}$ , which new decision she could pick?

**FTL:**  $x_t = \min_{x \in \mathcal{X}} \sum_{i=0}^{t-1} \ell_i(x)$ 

#### A no-regret algorithm: Follow-the-Leader

At time step t, learner has seen  $\ell_0, \ldots \ell_{t-1}$ , which new decision she could pick?

**FTL:**  $x_t =$ 

$$= \min_{x \in \mathcal{X}} \sum_{i=0}^{t-1} \ell_i(x)$$

Theorem (FTL): if  $\mathscr{X}$  is convex, and  $\mathscr{C}_t$  is strongly convex for all t, then for regret of FTL, we have:  $\frac{1}{T} \left[ \sum_{t=0}^{T-1} \ell_t(x_t) - \min_{x \in \mathcal{X}} \sum_{t=0}^{T-1} \ell_t(x) \right] = O\left(\frac{\log(T)}{T}\right)$ 





#### At iteration n:

#### **New Data**

















Aggregate  
Dataset  
$$\sum_{i=1}^{n} ||\pi(x) - y||_{2}^{2}$$
Aggregate  
$$\sum_{i=1}^{n} ||\pi(x) - y||_{2}^{2}$$

$$\sum_{i=1}^{n} ||\pi(x) - y||_{2}^{2}$$

At iteration n:



#### **Supervised Learning**



At iteration n:



Supervised Learning



At iteration n:



Supervised Learning

Data Aggregation = Follow-the-Leader Online Learner



Finite horizon episodic MDP, assume discrete action space

Decision set  $\Pi := \{\pi : S \mapsto A\}$  (restricted policy class,  $\pi^*$  may not be inside  $\Pi$ )

Online Learning loss at iteration

- Finite horizon episodic MDP, assume discrete action space
- Decision set  $\Pi := \{\pi : S \mapsto A\}$  (restricted policy class,  $\pi^*$  may not be inside  $\Pi$ )

on *t*: 
$$\ell_t(\pi) = \mathbb{E}_{s \sim d^{\pi_t}} \left[ \ell(\pi(s), \pi^*(s)) \right]$$

(Here  $\ell$  could be any convex surrogate loss for classification, .e.g, hinge loss)

Finite horizon episodic MDP, assume discrete action space

Decision set  $\Pi := \{\pi : S \mapsto A\}$  (restricted policy class,  $\pi^*$  may not be inside  $\Pi$ )

Online Learning loss at iteration

DAgger is equivalent to F

on t: 
$$\mathscr{C}_t(\pi) = \mathbb{E}_{s \sim d^{\pi_t}} \left[ \mathscr{C}(\pi(s), \pi^*(s)) \right]$$

(Here  $\ell$  could be any convex surrogate loss for classification, .e.g, hinge loss)

TL, i.e., 
$$\pi_{t+1} = \arg\min_{\pi \in \Pi} \sum_{i=0}^{t} \ell_i(\pi)$$

Finite horizon episodic MDP, assume discrete action space

Decision set  $\Pi := \{\pi : S \mapsto A\}$  (restricted policy class,  $\pi^*$  may not be inside  $\Pi$ )

Online Learning loss at iteration

DAgger is equivalent to F

If the online learning procedure ensures no-regret, then  $\frac{1}{T} \left[ \sum_{t=0}^{T-1} \ell_t(\pi_t) - \min_{\pi \in \Pi} \sum_{t=0}^{T-1} \sum_{t=0}^{T-1} \ell_{t}(\pi_t) - \min_{\pi \in \Pi} \sum_{t=0}^{T-1} \ell_{t}(\pi_t) - \ell_{T}(\pi_t) \right]$ 

on t: 
$$\ell_t(\pi) = \mathbb{E}_{s \sim d^{\pi_t}} \left[ \ell(\pi(s), \pi^*(s)) \right]$$

(Here  $\ell$  could be any convex surrogate loss for classification, .e.g, hinge loss)

TL, i.e., 
$$\pi_{t+1} = \arg\min_{\pi \in \Pi} \sum_{i=0}^{t} \ell_i(\pi)$$

$$\min_{\pi \in \Pi} \left[ \sum_{t=0}^{T-1} \ell_t(\pi) \right] = o(T)/T$$

Online Learning loss at iteration *t*:  $\ell_t(\pi) = \mathbb{E}_{s \sim d^{\pi_t}} \left| \ell(\pi(s), \pi^*(s)) \right|$  $\sum_{t=0}^{T-1} \ell_t(\pi_t) - \min_{\pi \in \Pi} \sum_{t=0}^{T-1} \ell_t(\pi) = o(T)$ 



Online Learning loss at iteration

 $\sum_{t=0}^{T-1} \ell_t(\pi_t) - \min_{\pi \in \Pi} \sum_{t=0}^{T-1} \sum_{t=0}^{T-1} \ell_{t=0}$ 

 $\frac{1}{T} \sum_{t=0}^{T-1} \ell_t(\pi_t) = o(T)$ 

on 
$$t$$
:  $\ell_t(\pi) = \mathbb{E}_{s \sim d^{\pi_t}} \left[ \ell(\pi(s), \pi^*(s)) \right]$   

$$\min_{t \in \Pi} \sum_{t=0}^{T-1} \ell_t(\pi) = o(T)$$

$$(T)/T + \min_{\pi \in \Pi} \frac{1}{T} \sum_{t=0}^{T-1} \ell_t(\pi)$$

$$\underbrace{\frac{1}{\pi e_{\Pi}} \sum_{\tau=0}^{T-1} \ell_{\tau}(\pi)}_{\epsilon_{\Pi}}$$

Online Learning loss at iteratic

 $\sum_{t=0}^{T-1} \ell_t(\pi_t) - \max_{\pi \in T} \tau_{t=0}$ 

$$\frac{1}{T}\sum_{t=0}^{T-1} \mathscr{C}_t(\pi_t) = \underbrace{o(T)/T}_{\epsilon_{avg-reg}} + \underbrace{\min_{\pi \in \Pi} \frac{1}{T}\sum_{t=0}^{T-1} \mathscr{C}_t(\pi)}_{\epsilon_{\Pi}}$$

on 
$$t$$
:  $\ell_t(\pi) = \mathbb{E}_{s \sim d^{\pi_t}} \left[ \ell(\pi(s), \pi^*(s)) \right]$   

$$\min_{e \in \Pi} \sum_{t=0}^{T-1} \ell_t(\pi) = o(T)$$

 $\exists \hat{t} \in [0, ..., T-1]$ , such that:  $\ell_{\hat{t}}(\pi_{\hat{t}}) \leq \epsilon_{avg-reg} + \epsilon_{\Pi}$ 

Online Learning loss at iteratic

 $\sum_{\substack{t=0}}^{T-1} \ell_t(\pi_t) - \max_{\pi \in T} \ell_t(\pi_t) - m_{\pi \in T}$ 

$$\frac{1}{T}\sum_{t=0}^{T-1} \mathscr{C}_t(\pi_t) = \underbrace{o(T)/T}_{\epsilon_{avg-reg}} + \underbrace{\min_{\pi \in \Pi} \frac{1}{T}\sum_{t=0}^{T-1} \mathscr{C}_t(\pi)}_{\epsilon_{\Pi}}$$

 $\exists \hat{t} \in [0, ..., T-1], suc$ 

Under the assumption that surrogate loss upper bounds zero-one loss:

 $\mathbb{E}_{s \sim d^{\pi_{\hat{t}}}}\left[\pi_{\hat{t}}(s) \neq \pi^{\star}(s)\right] \leq \mathbb{E}_{s \sim d^{\pi_{\hat{t}}}}\left[\pi_{\hat{t}}(s) \neq \pi^{\star}(s)\right]$ 

on 
$$t$$
:  $\ell_t(\pi) = \mathbb{E}_{s \sim d^{\pi_t}} \left[ \ell(\pi(s), \pi^*(s)) \right]$   
$$\min_{t \in \Pi} \sum_{t=0}^{T-1} \ell_t(\pi) = o(T)$$

ch that: 
$$\ell_{\hat{t}}(\pi_{\hat{t}}) \leq \epsilon_{avg-reg} + \epsilon_{\Pi}$$

$$\epsilon_{d^{\pi_{\hat{t}}}}\left[\ell(\pi_{\hat{t}}(s),\pi^{\star}(s))\right] \leq \epsilon_{avg-reg} + \epsilon_{\Pi}$$

 $\pi_i$  can predict  $\pi^*$  well under its own state distribution

 $\mathbb{E}_{s \sim d^{\pi_{\hat{t}}}}\left[\pi_{\hat{t}}(s) \neq \pi^{\star}(s)\right] \leq \mathbb{E}_{s \sim d^{\pi_{\hat{t}}}}\left[\ell(\pi_{\hat{t}}(s), \pi^{\star}(s))\right] \leq \epsilon_{reg} + \epsilon_{\Pi}$ 

 $\mathbb{E}_{s \sim d^{\pi_{\hat{t}}}}\left[\pi_{\hat{t}}(s) \neq \pi^{\star}(s)\right] \leq \mathbb{E}_{s}$ 

 $\pi_{\hat{i}}$  can predict  $\pi^{\star}$  well under its own state distribution

Let's turn this to the true performance under the cost function c(s, a)

$$\mathbb{E}_{s \sim d^{\pi_{\hat{t}}}}\left[\ell(\pi_{\hat{t}}(s), \pi^{\star}(s))\right] \leq \epsilon_{reg} + \epsilon_{\Pi}$$

 $\mathbb{E}_{s \sim d^{\pi_{\hat{t}}}}\left[\pi_{\hat{t}}(s) \neq \pi^{\star}(s)\right] \leq \mathbb{E}_{s}$ 

Let's turn this to the true performance under the cost function c(s, a)

$$V^{\pi_{\hat{i}}} - V^{\pi^{\star}} = \frac{1}{1 - \gamma} \mathbb{E}_{s \sim d^{\pi_{\hat{i}}}} \left[ A^{\star}(s, \pi_{\hat{i}}(s)) \right]$$

$$\mathbb{E}_{s \sim d^{\pi_{\hat{t}}}}\left[\ell(\pi_{\hat{t}}(s), \pi^{\star}(s))\right] \leq \epsilon_{reg} + \epsilon_{\Pi}$$

 $\pi_i$  can predict  $\pi^*$  well under its own state distribution

 $\mathbb{E}_{s \sim d^{\pi_{\hat{t}}}}\left[\pi_{\hat{t}}(s) \neq \pi^{\star}(s)\right] \leq \mathbb{E}_{s}$ 

Let's turn this to the true performance under the cost function c(s, a)

$$V^{\pi_{\hat{i}}} - V^{\pi^{\star}} = \frac{1}{1 - \gamma} \mathbb{E}_{s \sim d^{\pi_{\hat{i}}}} \left[ A^{\star}(s, \pi_{\hat{i}}(s)) \right]$$
$$= \frac{1}{1 - \gamma} \mathbb{E}_{s \sim d^{\pi_{\hat{i}}}} \left[ A^{\star}(s, \pi_{\hat{i}}(s)) - A^{\star}(s, \pi^{\star}(s)) \right]$$

$$\mathbb{E}_{s \sim d^{\pi_{\hat{t}}}}\left[\ell(\pi_{\hat{t}}(s), \pi^{\star}(s))\right] \leq \epsilon_{reg} + \epsilon_{\Pi}$$

 $\pi_{\hat{i}}$  can predict  $\pi^{\star}$  well under its own state distribution

 $\mathbb{E}_{s \sim d^{\pi_{\hat{t}}}}\left[\pi_{\hat{t}}(s) \neq \pi^{\star}(s)\right] \leq \mathbb{E}_{s}$ 

Let's turn this to the true performance under the cost function c(s, a)

$$V^{\pi_{\hat{i}}} - V^{\pi^{\star}} = \frac{1}{1 - \gamma} \mathbb{E}_{s \sim d^{\pi_{\hat{i}}}} \left[ A^{\star}(s, \pi_{\hat{i}}(s)) \right]$$
  
=  $\frac{1}{1 - \gamma} \mathbb{E}_{s \sim d^{\pi_{\hat{i}}}} \left[ A^{\star}(s, \pi_{\hat{i}}(s)) - A^{\star}(s, \pi^{\star}(s)) \right]$   
 $\leq \frac{1}{1 - \gamma} \mathbb{E}_{s \sim d^{\pi_{\hat{i}}}} \left[ \mathbf{1} \{ \pi_{\hat{i}}(s) \neq \pi^{\star}(s) \} \max_{s, a} \left| A^{\star}(s, a) \right| \right]$ 

$$\mathbb{E}_{s \sim d^{\pi_{\hat{t}}}}\left[\ell(\pi_{\hat{t}}(s), \pi^{\star}(s))\right] \leq \epsilon_{reg} + \epsilon_{\Pi}$$

 $\pi_{\hat{i}}$  can predict  $\pi^{\star}$  well under its own state distribution

 $\mathbb{E}_{s \sim d^{\pi_{\hat{t}}}}\left[\pi_{\hat{t}}(s) \neq \pi^{\star}(s)\right] \leq \mathbb{E}_{s}$ 

Let's turn this to the true performance under the cost function c(s, a)

$$V^{\pi_{\hat{i}}} - V^{\pi^{\star}} = \frac{1}{1 - \gamma} \mathbb{E}_{s \sim d^{\pi_{\hat{i}}}} \left[ A^{\star}(s, \pi_{\hat{i}}(s)) \right]$$
$$= \frac{1}{1 - \gamma} \mathbb{E}_{s \sim d^{\pi_{\hat{i}}}} \left[ A^{\star}(s, \pi_{\hat{i}}(s)) - A^{\star}(s, \pi^{\star}(s)) \right]$$
$$\leq \frac{1}{1 - \gamma} \mathbb{E}_{s \sim d^{\pi_{\hat{i}}}} \left[ \mathbf{1} \{ \pi_{\hat{i}}(s) \neq \pi^{\star}(s) \} \max_{s,a} \left| A^{\star}(s, a) \right| \right]$$
$$\leq \frac{\max_{s,a} \left| A^{\star}(s, a) \right|}{1 - \gamma} \cdot (\epsilon_{reg} + \epsilon_{\Pi})$$

$$\mathbb{E}_{s \sim d^{\pi_{\hat{t}}}}\left[\ell(\pi_{\hat{t}}(s), \pi^{\star}(s))\right] \leq \epsilon_{reg} + \epsilon_{\Pi}$$

 $\pi_{\hat{i}}$  can predict  $\pi^{\star}$  well under its own state distribution

 $\mathbb{E}_{s \sim d^{\pi_{\hat{t}}}}\left[\pi_{\hat{t}}(s) \neq \pi^{\star}(s)\right] \leq \mathbb{E}$ 

Let's turn this to the true performance under the cost function c(s, a)

$$V^{\pi_{\hat{i}}} - V^{\pi^{\star}} = \frac{1}{1 - \gamma} \mathbb{E}_{s \sim d^{\pi_{\hat{i}}}} \left[ A^{\star}(s, \pi_{\hat{i}}(s)) \right]$$
  
=  $\frac{1}{1 - \gamma} \mathbb{E}_{s \sim d^{\pi_{\hat{i}}}} \left[ A^{\star}(s, \pi_{\hat{i}}(s)) - A^{\star}(s, \pi^{\star}(s)) \right]$   
 $\leq \frac{1}{1 - \gamma} \mathbb{E}_{s \sim d^{\pi_{\hat{i}}}} \left[ 1\{\pi_{\hat{i}}(s) \neq \pi^{\star}(s)\} \max_{s,a} \left| A^{\star}(s, a) \right| \right]$   
 $\leq \frac{\max_{s,a} \left| A^{\star}(s, a) \right|}{1 - \gamma} \cdot (\epsilon_{reg} + \epsilon_{\Pi})$ 

$$\mathbb{E}_{s \sim d^{\pi_{\hat{t}}}}\left[\ell(\pi_{\hat{t}}(s), \pi^{\star}(s))\right] \leq \epsilon_{reg} + \epsilon_{\Pi}$$

 $\pi_i$  can predict  $\pi^*$  well under its own state distribution

#### **Case study:**

**1. Worst case:**  $A^{\star}(s, a) \approx \frac{1}{1 - \gamma}$  (not

recoverable from a mistake): quadratic dependence on horizon, i.e., no better than BC;

 $\mathbb{E}_{s \sim d^{\pi_{\hat{t}}}}\left[\pi_{\hat{t}}(s) \neq \pi^{\star}(s)\right] \leq \mathbb{E}$ 

Let's turn this to the true performance under the cost function c(s, a)

$$V^{\pi_{\hat{i}}} - V^{\pi^{\star}} = \frac{1}{1 - \gamma} \mathbb{E}_{s \sim d^{\pi_{\hat{i}}}} \left[ A^{\star}(s, \pi_{\hat{i}}(s)) \right]$$
  
=  $\frac{1}{1 - \gamma} \mathbb{E}_{s \sim d^{\pi_{\hat{i}}}} \left[ A^{\star}(s, \pi_{\hat{i}}(s)) - A^{\star}(s, \pi^{\star}(s)) \right]$   
 $\leq \frac{1}{1 - \gamma} \mathbb{E}_{s \sim d^{\pi_{\hat{i}}}} \left[ 1\{\pi_{\hat{i}}(s) \neq \pi^{\star}(s)\} \max_{s,a} \left| A^{\star}(s, a) \right| \right]$   
 $\leq \frac{\max_{s,a} \left| A^{\star}(s, a) \right|}{1 - \gamma} \cdot (\epsilon_{reg} + \epsilon_{\Pi})$ 

$$\mathbb{E}_{s \sim d^{\pi_{\hat{t}}}}\left[\ell(\pi_{\hat{t}}(s), \pi^{\star}(s))\right] \leq \epsilon_{reg} + \epsilon_{\Pi}$$

 $\pi_i$  can predict  $\pi^*$  well under its own state distribution

### **Case study: 1. Worst case:** $A^{\star}(s, a) \approx \frac{1}{1 - \gamma}$ (not recoverable from a mistake): quadratic dependence on horizon, i.e., no better than BC; 2. Good case: $A^{\star}(s, a) \approx o\left(\frac{1}{1}\right)$ (easily

recoverable from a one-step mistake): Better than BC;





 $1 - \gamma /$ 

1. Behavior Cloning (Maximum Likelihood Estimation)

Performance-gap  $\approx \frac{1}{(1-\gamma)^2}$  (classification error)

1. Behavior Cloning (Maximum Likelihood Estimation)

Performance-gap  $\approx -$ 

$$\frac{1}{(1-\gamma)^2}$$
 (classification error)

2. Hybrid Distribution Matching (w/ IPM or MaxEnt-IRL): Performance-gap  $\approx \frac{1}{(1-\gamma)}$  (classification error)

1. Behavior Cloning (Maximum Likelihood Estimation)

Performance-gap  $\approx -$ 

3.DAgger w/ Interactive Experts:

Performance-gap  $\approx \frac{\sup_{s,\iota}}{\iota}$ 

$$\frac{1}{(1-\gamma)^2}$$
 (classification error)

2. Hybrid Distribution Matching (w/ IPM or MaxEnt-IRL): Performance-gap  $\approx \frac{1}{(1-\gamma)}$  (classification error)

$$\frac{a|A^{\star}(s,a)|}{(1-\gamma)}$$
 (classification error)

### **Summary of the Course**

#### **Basics of MDPs (and LQRs):**

Planning: VI, PI, LP formulations, Fitted Q-iteration (under B-complete), Low bounds on linear  $Q^{\star}$ 


# Summary of the Course

### **Basics of MDPs (and LQRs):**

Planning: VI, PI, LP formulations, Fitted Q-iteration (under B-complete), Low bounds on linear  $Q^{\star}$ 

## Exploration in MDPs (bandit / tabular / linear mdp / Bellman rank):

Key intuition: optimism in the face of uncertainty



# Summary of the Course

#### **Basics of MDPs (and LQRs):**

Planning: VI, PI, LP formulations, Fitted Q-iteration (under B-complete), Low bounds on linear  $Q^{\star}$ 

## Exploration in MDPs (bandit / tabular / linear mdp / Bellman rank):

Key intuition: optimism in the face of uncertainty

### **Policy Gradient methods (tabular, linear, and neural)**

Global convergence of PG and NPG (if the reset distribution covers  $d^{\star}$ )



# Summary of the Course

#### **Basics of MDPs (and LQRs):**

Planning: VI, PI, LP formulations, Fitted Q-iteration (under B-complete), Low bounds on linear  $Q^{\star}$ 

## Exploration in MDPs (bandit / tabular / linear mdp / Bellman rank):

Key intuition: optimism in the face of uncertainty

### **Policy Gradient methods (tabular, linear, and neural)**

Global convergence of PG and NPG (if the reset distribution covers  $d^{\star}$ )

#### **Imitation Learning**

Distribution shift in offline IL and how we overcome it in the hybrid and interactive settings

